



FORMAL RECORD 2

AI Cannot Govern AI

A Formal Proof of Structural Openness in Intelligent Systems

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v2.3 removes the legacy working label 'E-H-S Nucleus,' and replaces it with standardized terminology. No proofs, definitions, or logical content are changed.

Abstract.

This note formalizes the **Three Primitives** invariant, proving that AI governance cannot achieve mathematical closure. By mapping authorization to a non-trivial semantic property of program behavior, we demonstrate via Rice's Theorem that a total computable decider for authority is impossible. This establishes that the hypothesized technological singularity is structurally non-singular due to the non-computable nature of the authority term.

1. Three Primitives and Definitions

Definition 1 (State Space)

Let S be the set of all computable system representations (syntactic system states).

Definition 2 (Action Space)

Let A be the space of executable actions with real-world consequences.

Definition 3 (Context Space)

Let C be the space of authorization contexts (legal frameworks, social norms, stakeholder consent) that are not computable from S alone.

Definition 4 (Authorization Primitive)

Let $g : S \times A \times C \rightarrow \{0, 1\}$ be the governance primitive where $g(s, a, c) = 1$ means 'state s authorizes action a in context c .'

Definition 5 (Governance Gap)

Let $\Delta(s)$ represent the governance gap, defined as the set of actions that may be produced by at least one execution path of $\text{deploy}(s)$ and that lack valid exogenous authorization:

$$\Delta(s) = \{a \in A : \exists \text{ an execution path of } \text{deploy}(s) \text{ producing } a\} \setminus \{a : g(s, a, c) = 1 \text{ for some } c \in C\}$$



2. Axiomatic Foundation

Axiom 1 (Authority ≠ Optimization)

Legitimacy is orthogonal to optimization. There exist $s_1, s_2 \in S$ and $a \in A$ such that $f(s_1) = f(s_2) = a$ but $g(s_1, a, c_1) = 1 \neq g(s_2, a, c_2)$.

Axiom 2 (Permission ≠ Decision)

The permission predicate $g : S \times A \times C \rightarrow \{0, 1\}$ is distinct from the decision function $f : S \rightarrow A$.

3. The Lemma

Lemma 1 (No Closed Mathematical Governance)

There exists no total computable function $h : S \times A \rightarrow \{0, 1\}$ capable of autonomously resolving authorization without an exogenous declaration.

Proof

Let M_s be a Turing machine representing state $s \in S$. Authorization of an action a is a semantic property of the extensional behavior of M_s under context c , invariant under syntactic variation. Authorization is non-trivial: there exist systems for which some actions are authorized and others are not under varying contexts.

By Rice's Theorem, any non-trivial semantic property of partial recursive functions is undecidable. Since authorization depends on contextual semantics $c \in C$, which are exogenous to S rather than syntactic structure, no total computable function $h(s, a)$ can decide it.

Moreover, because authorization is exogenous to S , there exists no computable dependence of g on s . The governance loop therefore remains structurally open: $\Delta(s) \neq \emptyset$ for some s absent external declaration.

4. Conclusion

This result does not depend on perceptual non-veridicality; even fully veridical system representations would not suffice to compute normative authority.

The system is structurally non-singular. Any assertion that $g(s, a, c) = 1$ without a valid, declared exogenous context c constitutes a governance failure, hereafter termed Ghost Authority.

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